

$$c) \quad S = \int_0^{\frac{2\pi}{\omega}} |V(t)| dt \rightarrow \int_0^{\frac{2\pi}{\omega}} \sqrt{8R^2\omega^2(1+\cos(3\omega t))} dt$$

$$= \left[\sqrt{8R^2\omega^2(1+\cos(3\omega t))} t \right]_0^{\frac{2\pi}{\omega}} = \sqrt{8R^2\omega^2(1+\cos(3\omega t))} \frac{2\pi}{\omega}$$

$$s = |V(t)| \cdot t \quad \Leftrightarrow \quad t = \frac{s}{|V(t)|}$$

$$\frac{1}{t} = \frac{d\vec{r}(s)}{ds}$$

$$\vec{n} = \frac{\frac{d\vec{r}(s)}{ds}}{\left| \frac{d\vec{r}}{ds} \right|} = \frac{1}{k} \frac{d\vec{r}}{ds}$$

$$\vec{r}(s) = 2R \begin{pmatrix} \cos\left(\frac{\omega s}{|V(t)|}\right) - \cos^2\left(\frac{\omega s}{|V(t)|}\right) \\ \sin\left(\frac{\omega s}{|V(t)|}\right) - \sin\left(\frac{\omega s}{|V(t)|}\right) \cdot \cos\left(\frac{\omega s}{|V(t)|}\right) \end{pmatrix}$$

$$\frac{d\vec{r}(s)}{ds} = 2R \begin{pmatrix} -\frac{\omega}{|V(t)|} \sin\left(\frac{\omega s}{|V(t)|}\right) + \frac{2\omega \sin\left(\frac{\omega s}{|V(t)|}\right) \cdot \cos\left(\frac{\omega s}{|V(t)|}\right)}{|V(t)|} \\ \frac{\omega}{|V(t)|} \cos\left(\frac{\omega s}{|V(t)|}\right) - \frac{\omega}{|V(t)|} \cos^2\left(\frac{\omega s}{|V(t)|}\right) + \frac{\omega}{|V(t)|} \sin^2\left(\frac{\omega s}{|V(t)|}\right) \end{pmatrix}$$

Hint:
 - A range + time

$$\frac{d\vec{r}(s)}{ds} = \frac{2R\omega}{|V(t)|} \begin{pmatrix} -\sin\left(\frac{\omega s}{|V(t)|}\right) + \sin\left(2\frac{\omega s}{|V(t)|}\right) \\ \cos\left(\frac{\omega s}{|V(t)|}\right) + \cos\left(2\frac{\omega s}{|V(t)|}\right) \end{pmatrix}$$

$$\vec{e}_T(s) = \frac{2R\omega}{|V(t)|} \begin{pmatrix} -\sin\left(\frac{\omega s}{|V(t)|}\right) + \sin\left(2\frac{\omega s}{|V(t)|}\right) \\ \cos\left(\frac{\omega s}{|V(t)|}\right) + \cos\left(2\frac{\omega s}{|V(t)|}\right) \end{pmatrix}$$

$$k = \left| \frac{d\vec{r}(s)}{ds} \right| = \frac{2R\omega}{|V(t)|} \begin{pmatrix} -\frac{\omega}{|V(t)|} \cos\left(\frac{\omega s}{|V(t)|}\right) + \frac{2\omega}{|V(t)|} \cos\left(2\frac{\omega s}{|V(t)|}\right) \\ -\frac{\omega}{|V(t)|} \sin\left(\frac{\omega s}{|V(t)|}\right) - \frac{2\omega}{|V(t)|} \sin\left(2\frac{\omega s}{|V(t)|}\right) \end{pmatrix}$$

$$= \frac{2R\omega^2}{|V(t)|^2} \begin{pmatrix} -\cos\left(\frac{\omega s}{|V(t)|}\right) + 2\cos\left(2\frac{\omega s}{|V(t)|}\right) \\ -\sin\left(\frac{\omega s}{|V(t)|}\right) - 2\sin\left(2\frac{\omega s}{|V(t)|}\right) \end{pmatrix}$$

A1)

$$\left| \frac{e(t)}{ds} \right| = \sqrt{\frac{2R^2 \omega^4}{|V(t)|^4} \left(\cos^2\left(\frac{\omega s}{|V(t)|}\right) - 4 \cos\left(\frac{\omega s}{|V(t)|}\right) \cos\left(2\frac{\omega s}{|V(t)|}\right) + \cos^2\left(2\frac{\omega s}{|V(t)|}\right) + \sin^2\left(\frac{\omega s}{|V(t)|}\right) + 4 \sin\left(\frac{\omega s}{|V(t)|}\right) \sin\left(2\frac{\omega s}{|V(t)|}\right) + 4 \sin^2\left(2\frac{\omega s}{|V(t)|}\right) \right)}$$

$$= \sqrt{\frac{4R^2 \omega^4}{|V(t)|^4} \left(\underbrace{\cos^2\left(\frac{\omega s}{|V(t)|}\right) + \sin^2\left(\frac{\omega s}{|V(t)|}\right)}_1 + 4 \left(\underbrace{\sin\left(2\frac{\omega s}{|V(t)|}\right) + \cos\left(\frac{\omega s}{|V(t)|}\right)}_1 \right) - 4 (\cos(\alpha)\cos(\beta) - \sin(\alpha)\sin(\beta)) \right)}$$

$$k = \sqrt{\frac{4R^2 \omega^4}{|V(t)|^4} \left(5 - 4 \cos\left(3\frac{\omega s}{|V(t)|}\right) \right)}$$

$$\vec{e}_N = \frac{e(t)}{ds} \Rightarrow \frac{2R\omega^2}{|V(t)|^2} \begin{pmatrix} -\cos\left(\frac{\omega s}{|V(t)|}\right) + 2\cos\left(2\frac{\omega s}{|V(t)|}\right) \\ -\sin\left(\frac{\omega s}{|V(t)|}\right) - 2\sin\left(2\frac{\omega s}{|V(t)|}\right) \end{pmatrix}$$

$$\frac{2R\omega^2}{|V(t)|^2} \sqrt{5 - 4 \cos\left(3\frac{\omega s}{|V(t)|}\right)}$$

$$p = \frac{1}{k} \rightarrow \frac{|V(t)|^2}{2R\omega^2 \sqrt{5 - 4 \cos\left(3\frac{\omega s}{|V(t)|}\right)}}$$

$$a = \underbrace{\frac{d|V(t)|}{dt}}_0 \vec{e}_T + \frac{|V(t)|^2}{p} \vec{e}_N$$

$$\frac{(8R^2 \omega^2 (1 + \cos(3\omega t))) 2R\omega^2 \sqrt{5 - 4 \cos\left(3\frac{\omega s}{|V(t)|}\right)}}{(8R^2 \omega^2 (1 + \cos(3\omega t)))}$$

$$\begin{pmatrix} -\cos\left(\frac{\omega s}{|V(t)|}\right) + 2\cos\left(2\frac{\omega s}{|V(t)|}\right) \\ -\sin\left(\frac{\omega s}{|V(t)|}\right) - 2\sin\left(2\frac{\omega s}{|V(t)|}\right) \end{pmatrix} \sqrt{5 - 4 \cos\left(3\frac{\omega s}{|V(t)|}\right)}$$

sieht wie $a(t)$ aus
nur statt ωt , ist es s

$\frac{\omega s}{|V(t)|}$! Ist dies dann
wirklich gleich?

Ich kann das nicht
weiter auflösen!